

A comprehensive study of process calculi with routing tables

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Abstract

In this paper, we have described the research carried out in formal modeling of distributed networks in a process algebraic framework. The extended version of asynchronous distributed π -calculus named as routing calculi, DR_{π}^{ω} and DR_{π} were the one of the significant developments towards modeling the distributed computer network using the router as an active component and considering the path of communication between the communicating nodes where a routing table is a dynamic entity in a typical distributed network. In formal modeling, the routing tables was updated upon creation of the new node in the network, but already existing entries in the routing table remain unchanged. We have done a comprehensive study of previous year's research in this area on the basis of which we derive our motivation with an intention to extend the existing routing calculi DR_{π}^{ω} to incorporate the dynamic updates of the routing table through the distance routing protocol. It has adaptive features based upon the network parameter changes. This model is closer to the real networks. These calculi are primarily considered as a metric to determine the quality of services (QoS).

Keywords

Routing calculi, Process calculi, π -calculus, Routing protocols.

1.Introduction

With the evolution of large system over distributed computing environment, the need of verifying and validating the system becomes an important concern. The researches in theories of computing come up with the idea of process calculi like calculus of communicating system (CCS), communicating sequential processes (CSP), algebra of communicating processes (ACP) and language of temporal ordering specification (LOTOS). These are the major branches of the process calculi. Main research is started with Milner's work on the CCS [1] which is mainly based on observation bisimulation that defines communication between processed for the system. CSP by Hore's work [2] defines a specific calculus for defining a system and investigate to find correctness with its operational semantics and bisimulation. ACP [3] by Bergstra and Klop investigate the solutions of system equation, operational semantics and bisimulation. Finally, LOTOS [4], is a formal specification calculus, is used for protocol specification in ISO standards.

Process calculi is a useful framework which is used in the study of concurrent and distributed system. One of the most popular calculus, the π -calculus [1, 5–8] of Milner, Parrow, and Walker is a simple and powerful calculus which describes the behavior of concurrent systems. A large amount of research work has been carried to define various application of process calculi in different system as the applied calculus [9] and the spi-calculus [10–12] have been used to study security protocol, the ambient calculus [13] defines mobile computations, the join calculus [14] has been used as basis for distribute implementations, the distributed π -calculus [15] for controlling the access to resources, the π_{cost} [16,17] defines cost function which calculates the cost of communication between the processes and the routing calculus [18] for distributing computing. Recently work on process calculi can be seen in [19–29].

We present an account of all these [30, 31] calculi to demonstrate both their features and limitation. Based upon the above discussion, we drive a motivation to develop a new routing calculi which can overcome one of the limitations of existing calculi to improve the QoS the formally described distributed network

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and then modeling this new development close to the real distribute network.

Further, this paper has been organized in six sections. In section 2, we describe related work for routing calculi in distributing computing. In section 3 comparative analyses has been described for process calculi. In section 4 and section 5, motivation and methodology have been discussed respectively. Finally, concluding section has been included in section 6.

2.Related work

Here in this section, we briefly describe some calculi that are relevant to the research problem. For this we describe asynchronous π -calculus, adding the cost in the π -calculus and routing calculus for distributed computing.

2.1Asynchronous π -calculus

Asynchronous π -calculus [5, 8, 32] is a computational and simple model for concurrent system [1]. In asynchronous π -calculus, the two concurrent processes can interact by sending values through communication links to each other i.e. where values can be interchanged between concurrent processes in a completely asynchronous manner through communication channels. These channels can be declared for the private use of a specific process. The syntax of the asynchronous π -calculus is as follows:

$$R ::= \text{stop} \mid u! \langle v \rangle \mid u?(x) R \mid (\text{new } n) R \mid R_1 \mid R_2$$

Here the simplest possible process, which does nothing, is stopped. The output of a value is represented by the term $u! \langle v \rangle$ that transmits the value v asynchronously via channel u . The term $u?(x)R$ represents a term which can input a value along the channel u where x is the variable for the value to be communicated with the process R . If $v_1 = v_2$ then R_1 else R_2 is the test for the identity of simple values. $(\text{new } n) R$ is used for scoping of names. $R_1 \mid R_2$ are running in parallel. Where R_1 and R_2 are two processes.

2.2D $_{\pi}$: Distributed π -calculus

The extension of π -calculus is asynchronous Distributed π -calculus [15] which is represented as D_{π} . Here the distributed system is viewed as a collection of domains, each capable of hosting computational processes, which in turn can migrate between domains. The topology of the communicating nodes is a clique of the graph which is not the case in the realistic distributed network. In distributed π -calculus system is defined as:

$$l \llbracket p_1 \rrbracket (\text{new } e: D) (k \llbracket Q \rrbracket \mid l \llbracket P_2 \rrbracket)$$

Here, these are three located processes or agents where P_1 is running at location l , Q is running at location k and P_2 is running at location l . e is common resource which is a common sharing of type D . The new addition to the syntax of processes of this language is a migration which is represented as *goto* k . P meaning the running at any location l with migrate to location k where the code P is launched. Others are channel name creation and new location name creation. In this language, there are not a direct connection between this formal syntax for the system by using parallel contractor \mid and new name constructor $(\text{new } e: D) (-)$. The axioms are inherited from the reduction semantics for asynchronous π -calculus and now they are being applied to locate processes. The new migration rule [15] is represented as $k \llbracket \text{goto } l . P \rrbracket \rightarrow l \llbracket P \rrbracket$.

2.3 π_{cost} : adding the cost in the π -calculus

π_{cost} [16, 17] is a simple language which is another variation of asynchronous π -calculus [5, 8, 32] where values can be exchanged between the concurrent processes in a completely asynchronous manner via communication channels that can be declared as private. The most important modification with respect to asynchronous π -calculus is a cost function which calculates the cost of communication between the processes in a distributed network (defined over channel names). The cost function is calculated with the number of hops as the message is passed between the nodes.

In π_{cost} the syntactical representation of reduction semantic is $c \vdash P \rightarrow^n c \vdash Q$ where a process P reduces to another process Q . The cost of this reduction is n which is defined by the cost function c . $c \vdash P$ is defined as a system. Another most important modification with respect to asynchronous π -calculus is that the author has added a syntactic construct called delivery message i.e. *del* (b, u) which delivers a value u at channel b of a waiting input process. This is a delivery message which is produced by an output process.

2.4DR $_{\pi}^{\omega}$, DR $_{\pi}$: a routing calculus for distributed computing

Routing calculi [18] is a language that is a tertiary extension of typical asynchronous distributed π -calculus [15]. The network topology is defined as networks of routers considering router as a fixed entity. There are nodes that are connected to a router and the processes reside in nodes.

The extended version of asynchronous distributed π -calculus named as two routing calculi i.e. DR_{π}^{ω} [30] and DR_{π} [31] were the first significant development towards modeling the distributed compute network using router and considering the path between the communication nodes. Systems, nodes and processes are three main syntactic categories in the language.

This language has syntactic expressions of the form $\Gamma_c \triangleright (R)n [P]$ Where Γ_c is a router connectivity, (R) is a fixed routing table which hosts not n where process P resides in it and executes reduction of processes with respect to fixed router connectivity (which in not a clique of graph). The path can be determined by the routing table where entries are dynamically updated upon creation of new nodes. Upon creation of new nodes, the author has described two methods of updating routing tables, one method is flooding [33] and the other method is backward learning updates [34].

We describe the routing calculi incorporating backward learning updates and flooding updates as follows:

1. DR_{π}^{ω} : Updating router via a routing calculus with backward learning updates

Upon the creation of new nodes, the author has described a method of updating routing table [30]. In backward learning, tables are updated only when the

new node name in propagating message and delivery of values occurs. The routing tables determine the path communication along which the value to be communicated determine. The entries in the routing table are very much dependent on router connectivity. The main purpose of using this method is to determine the path. The routers maintain a table which can determine the next on the path towards the destination node at some router where the destination process runs. Every router has a routing table and is represented as (R) which consists of set of node names and its adjacent set of router names.

For example, in *Figure 1*, If a process at node a, which is router R_1 wants to communicate with a process at another node g which is at R_3 then router table (R_1) may return the adjacent router R_2 as next hop the communication path to g at R_3 . This may be formally expressed as $(R_1)(g) = R_2$. Similarly, the next router R_2 may decide that the next router for communication with g is R_3 . This may be determined using the routing table (R_2) at R_2 as an application of the routing table function. In another words $(R_2)(g) = R_3$. Author describes the notation $Adj(R)$ to represent the set of neighboring routers of R in Γ_c . Routing table is represented as:

$$Adj(R) = R' | (R, R') \in \Gamma_c$$

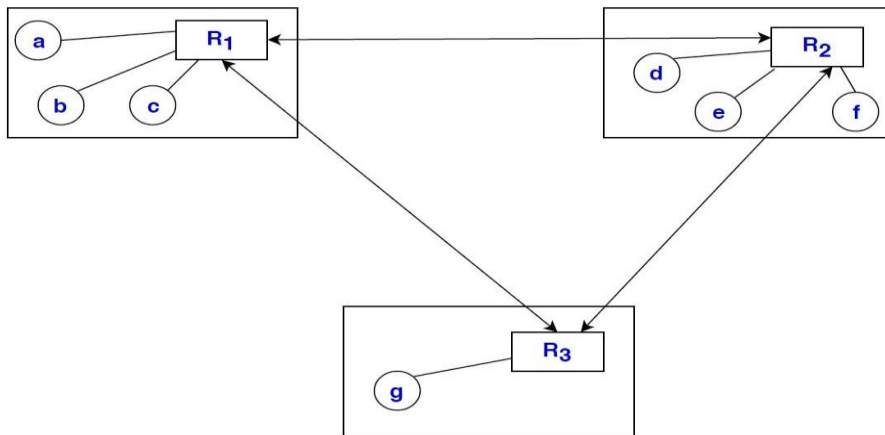


Figure 1 Sample distributed with routers and nodes

2. DR_{π} : Updating routers via routing calculus with flooding updates

Gaur et al. [31] describes that upon creation of a new node, a routing table is updated and information is broadcasted to all the connected routers and the routing tables are updated in updated in breadth-first traversal manner. Also generates two types of

messages, firstly control message for updating routing table and secondly the value propagating message that is used to deliver value to waiting input process. With the help of the reduction semantics of this language, it can be confirmed that no router table is left without the knowledge about the new node after which the update messages get terminated. This

method to update the routing table is known as flooding which is represented as DR_{π} [31].

The following table describes different parameters for showing the advantages and limitation of pervious and proposed calculi. It is also to consider that the following calculi are computational in nature.

3.Comparative analysis

Table 1 Comparison between process algebras

Process calculi	Node representation	Connectivity	Routing table (Y/N)	Path changes	Node to not connectivity
D_{π}	-	$goto k.P$	N	Static	Bidirectional
π_{cost}	-	$del(b, u)$	N	Static	Bidirectional
DR_{π}^{ω}	$n [T]$	Γ_c	Y	Static	Bidirectional
DR_{π}	$m [T]$	Γ_c	Y	Static	Bidirectional
Proposed calculi (DR_{π})	-	Γ_c	Y	Static	Bidirectional

This table has been concluded in the next section.

4.Motivation

With the comparative analysis, which is given in *Table 1*, it is clear that the extended version of asynchronous distributed π -calculus [15] for routing calculi i.e. DR_{π}^{ω} [30] and DR_{π} [31] were the significant development towards modeling the distributed computer network using an active component named router. Considering the path of a communication between the communicating nodes where a routing table is a dynamic entity in a typical distributed network. After conducting an extensive survey, we discovered the two different calculi for routing table updates have considered static that has been explained in our previous section. In this calculus, the routing table is updated only when a new node is created which limited dynamic updates of the table. In formal modeling it is a constant endeavor of the researcher of formally describes it as close as possible to the real distributed network. With this motivation a research problem can be formulated. Therefore, we propose to develop a new calculi which will be an extension of routing calculi, DR_{π}^{ω} [30] to incorporate the following features and thereby overcoming limitation of previous calculi.

- Optimal route choices based upon dynamic parameters of the network [35].
- Dynamic update of routing tables to implement standard methods such as DVR [36, 37] and link state [38].

5.Methodology

We extend the existing calculi to incorporate the dynamic updates of routing table via distance vector routing [36, 37]. Distance Vector is a proactive routing protocol, which continuously maintains the topological information and such route information is available immediately whenever communication is needed. In distance vector router exchanges information about the network with their neighboring nodes by sending their routing table and router periodically transmits the routing table via a broadcast packet that reaches all other routers on the local segments. Thus, the router updates the routing table. Distance vector routing protocols use the Bellman-Ford algorithm [33] to compute the shortest route. Routing updates are done step by step from route to route in *Figure 2*.

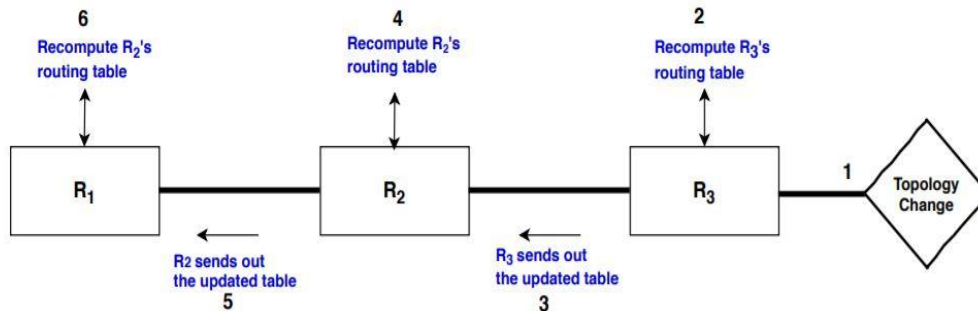


Figure 2 DVR: update routing information

Based on the limitation of previous work an extension of routing calculi with explicit features on routing table updates using a distance vector routing method have been developed [39]. This requires additional semantics rules. The challenges such as inconsistencies in simultaneous routing table are addressed. To ensure that all network properties are satisfied. We also define well-formed configurations. To justify our routing calculi, we take two routing calculi DR_{π}^{ω} [30] and DR_{π} [31] as its specification and show that both specifications conforms to its implementation which is our newly developed

calculi. In *Figure 3*, we define the methodology of proposed calculus, which is stated as:

1. It shows reduction equivalence with DR_{π} (Distributed π -calculus) [15] abstracted away the unnecessary details of implementations [30].
2. Showing bisimulation equivalence over labelled transition system (LTS) [40] of the calculi to an equivalence defined purely in the observational properties of the calculi. (Full abstraction) [15, 30, 41]

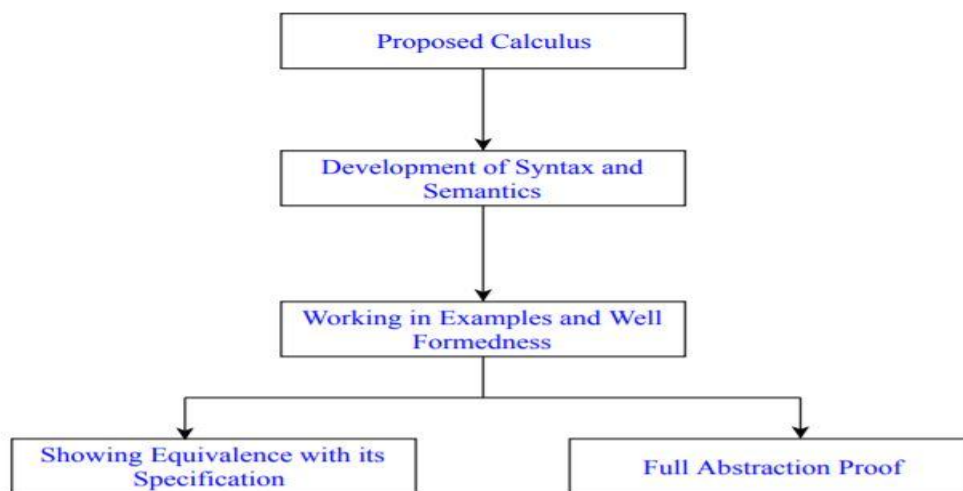


Figure 3 Methodology for proposed calculus

6. Conclusion

In this paper we have discussed various process calculi for routing in distributed system. Most of these researches had verified with the help of simulation tools such as a mobility workbench (MWB) [42], UPPAAL [43], simple promela interpreter (SPIN) [44] and LUNAR etc. The simulation tools had some limitation like qualitative aspects and other routing problems. Thus, the simulation tools could not be used to verify these systems by exploring all conditions related to them. Using formal methods, to overcome this situation, this system can be verified using theorem proven. That is why we can use the process algebraic framework. We observed in an existing routing calculus, the routing table (R) is a fixed table where as a routing table is a dynamic entity is a typical distribute network. In formal modeling, it is a constant endeavor of researcher to formally describe it as close as possible to the real distributed network. With this motivation, we extend the existing routing calculi to incorporate the dynamic updates of the

routing table. As a prototype we can incorporate distance vector routing where the adjacent routes exchange their routing table to obtain an optimal path description. The syntax and semantics of the existing routing calculi are proposed in [39]. We seek to design an extension of the routing calculi to incorporate the features of distance routing protocol [36] which has an adaptive feature based upon the network parameter changes. Distance vector routing [36] has less computational complexity and message overhead.

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Conflicts of interest

The authors have no conflicts of interest to declare.

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